# A Course on Meta-Heuristic Search Methods for Combinatorial Optimization Problems

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## Outline

- Genetic algorithm
- 2 Scatter search
- Artificial Immune System
  - Natural Immune System
- 4 Assignment





- Multi-parent crossover: http://citeseerx.ist.psu.edu/ viewdoc/download?doi=10.1.1.56.5147&rep=rep1&type=pdf
- Cellular GA: http://citeseerx.ist.psu.edu/viewdoc/ download?doi=10.1.1.65.7785&rep=rep1&type=pdf
- EA for VRP: http://citeseerx.ist.psu.edu/viewdoc/ download?doi=10.1.1.3.7230&rep=rep1&type=pdf





# Developed by Glover (1977)

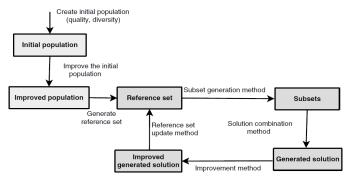


Figure: Flow chart of scatter search





#### Initial population:

- Generate a set of diverse and high quality solutions.
- Use a greedy procedure

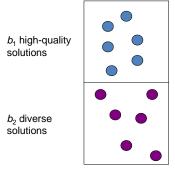
#### Improve initial population:

- Use a local search procedure.
- A Single-objective meta-heuristic can also be applied.





#### Reference set:



RefSet of size b Reference set





#### Subset generation method:

- Each subset should contain t solutions (t: size of subsets = 2).
- Each subset should include atleast one new solution.

#### Recomibination method:

- Recombine solutions in each subset.
- Any crossover operator can be used.

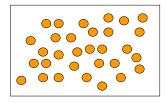




Reference set update: Combine sets and select the top best individuals.



RefSet of size b



Pool of new trial solutions

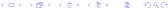




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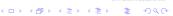
- Genetic algorithm
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### Overview

- It protects organisms from *pathogens* with several layers of defence.
- Surface barrier:
  - Skin, Hair
  - Body fluids: tears, sweat, etc.
- Innate immune system (non-specific response):
  - First arm A group of 20 proteins called the *complement system*. These proteins flow freely in the body. They kill invaders or recruit eater cells such as macrophages (a type of Phagocyte cell).
  - Second arm Phagocyte cells: They patrol the body searching for pathogens. If found, they eat and destroy them.
    - Third arm NK-cells: They kill virus-infected cells.



#### continue...

- Adaptive immune system (specific response):
  - Lymphocytes: T-cells and B-cells
  - T-cells:
    - Helper T-cells: Help B-cells and activate killer T-cells
    - Killer T-cells: kills infected cells.
  - B-cells: Once a B-cell finds an antigen matching its receptor, it becomes active. With the help of proteins of helper T-cells, it becomes fully active and proliferates into plasma cells and memory cells.





#### continue...

#### B-cell:

- Plasma cells: They produce specific antibodies that lock onto the antigen. Eater cells then chew up bacteria marked with antibodies.
- Memory cells: They memorizes specific intruders and helps the immune system to respond faster if the same intruder enters again.





# Basic principles

- Fit B-cells are allowed to grow in number.
- Unfit B-cells are slowly removed.
- Cloning is directly proportional to the fitness.
- Mutation is inversely proportional to the fitness.





# Working process

```
Template of the CLONALG.
```

**Input:** Initial population  $P_0$ .

 $P=P_0$ ; /\* Generation of the initial population of random antibodies \*/

#### Repeat

Evaluate all existing antibodies and compute their affinities;

Select N% of antibodies with highest affinities;

Clone the selected antibodies:

Maturate the cloned antibodies;

Evaluate all cloned antibodies:

Add R% of best cloned antibodies to the pool of antibodies;

Remove worst members of the antibodies pool;

Add new random antibodies into the population;

Until Stopping criteria satisfied

Output: Best population found.





$$N_c = \lfloor \frac{\beta \times |P_o|}{i} + 0.5 \rfloor \tag{3.1}$$

 $\beta \in [0,1]$ 

 $|P_o|$ : size of the population.

*i*: rank of an antibody in the sorted population according to ascending values of affinities.



## Assignment-II

- Form a group of 2 new students.
- Implement Genetic Algorithm algorithm on the single-variable Ackley function using C++/MATLAB/Java.
- Prepare a report of 3-5 pages (extend if needed):
  - Compare its performance against the Simulated Annealing algorithm.
  - Support your claims by:
    - Providing tables showing results on different values of algorithmic parameters (population size and crossover/mutation probability).
    - Providing graphs showing convergence of algorithm (w.r.t. number of iterations/computational time).
- Use population of binary strings.
- Use one/two point crossover.
- Use flip operator mutation.
- 10 experiments with different values of GA parameters.
- 20 runs for each parameter settings.
- Show results of the best run only.



Genetic algorithm Scatter search Artificial Immune System Assignment References

Glover, F. (1977). Heuristics for integer programming using surrogate constraints. *Decision Sciences*, 8(1):156–166.

