

**UNIVERSITÀ DEGLI STUDI ROMA TRE**  
Dipartimento di Informatica e Automazione

**Algorithms for the Inference of the  
Commercial Relationships between  
Autonomous Systems: Results  
Analysis and Model Validation**

**Massimo Rimondini**  
Maurizio Pizzonia  
Giuseppe Di Battista  
Maurizio Patrignani

# Summary

- ➔ Introduction
  - ◆ Motivations
  - ◆ Methodology
  - ◆ Tools
  - ◆ Experimental Results
  - ◆ Conclusions

# Introduction

## ◆ Autonomous System

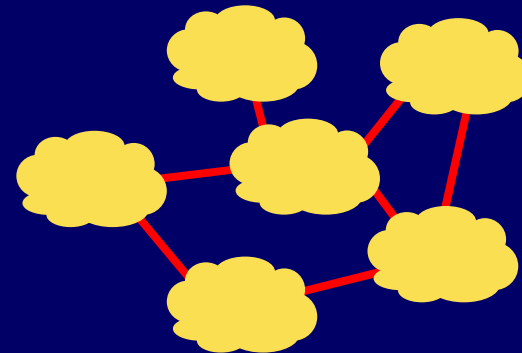
- (very) large set of network devices
  - under the control of a single administration
  - using coherent routing policies

## ◆ ASes exchange routing information using the Border Gateway Protocol

- BGP-speaking routers establish *peering sessions*
- the spread of BGP reachability messages can be limited using *policies*

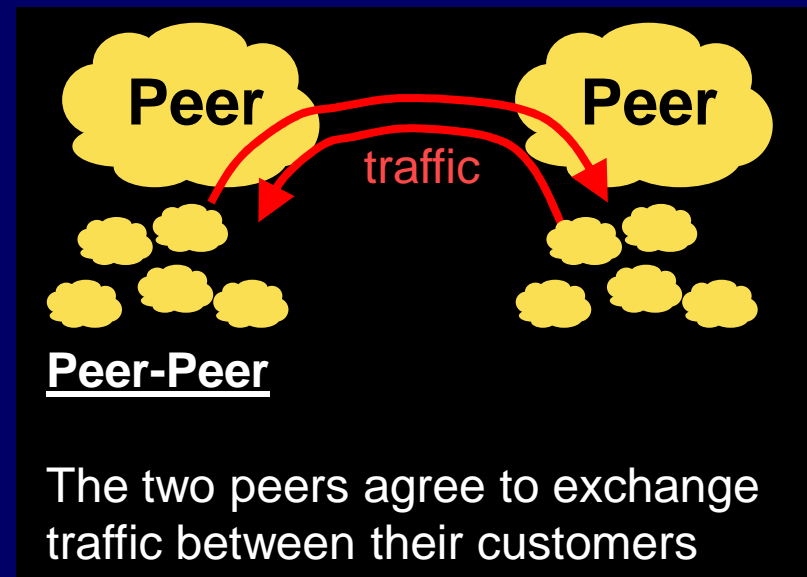
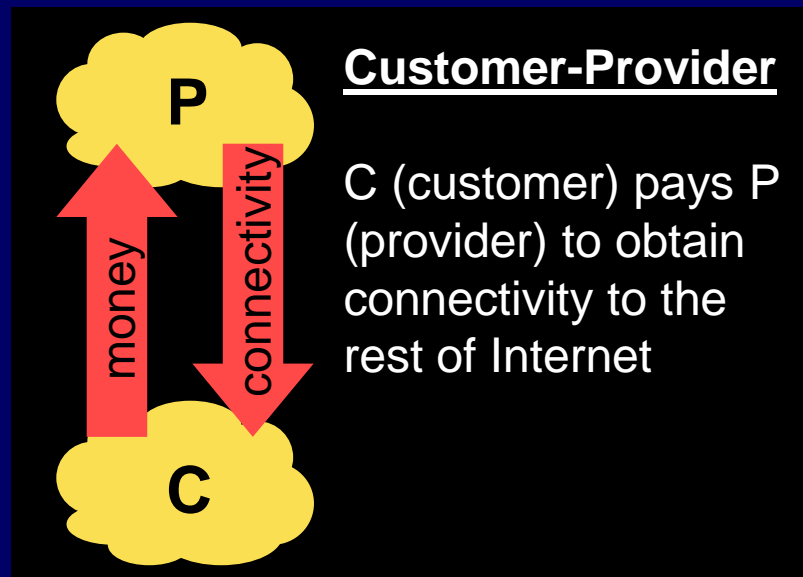
## ◆ Internet model

- interconnection of ASes



# Commercial Relationships

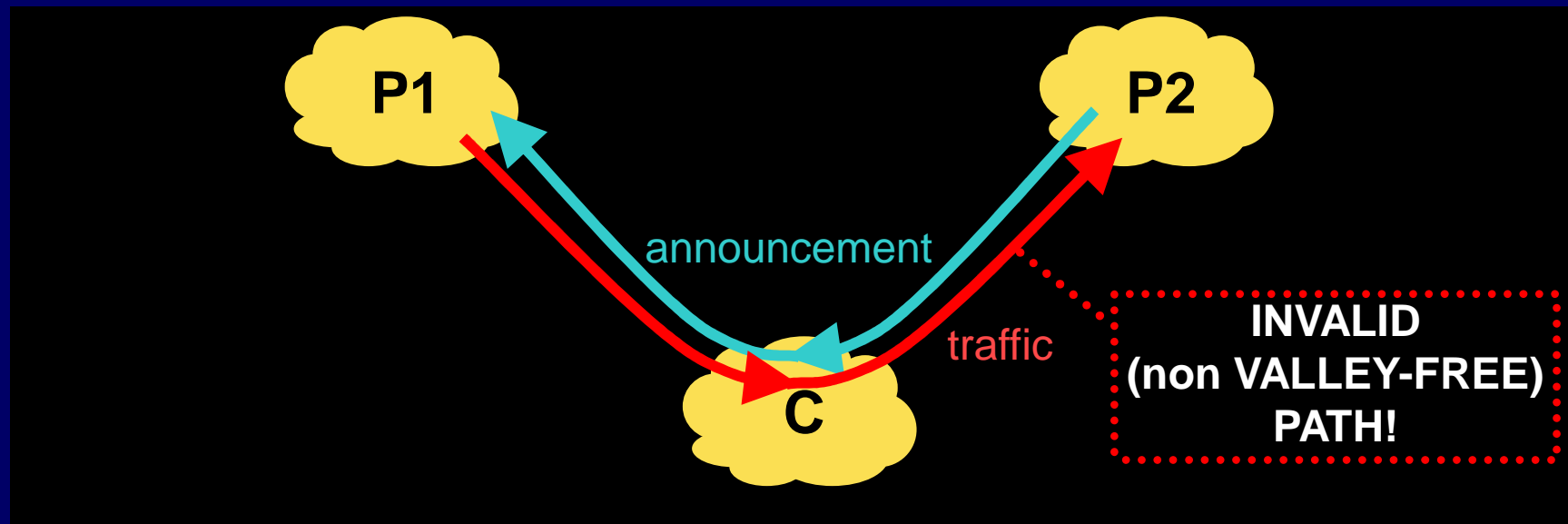
- ◆ Contracts which are subscribed in order to obtain connectivity
- ◆ Implemented by using BGP policies [1]



[1] Lixin Gao. On Inferring Autonomous System Relationships in the Internet.  
*IEEE/ACM Transactions on Networking*, 9(6):733–745, Dec 2001.

# Commercial Relationships

- ◆ Contracts which are subscribed in order to obtain connectivity
- ◆ Implemented by using BGP policies [1]



[1] Lixin Gao. On Inferring Autonomous System Relationships in the Internet. *IEEE/ACM Transactions on Networking*, 9(6):733–745, Dec 2001.

# Why using Inference Algorithms

- ✦ Knowing the commercial relationships is useful, but difficult
- ✦ Asking AS authorities for the commercial relationships they establish is unfeasible
  - too numerous
  - not willing to reveal sensible information
- ✦ Routing registries may be incomplete/out of date

# Inference Algorithms

- ◆ Inference algorithms take as input BGP routing data
- ◆ Produce as output a relationship assignment

- ◆ Network model: AS graph

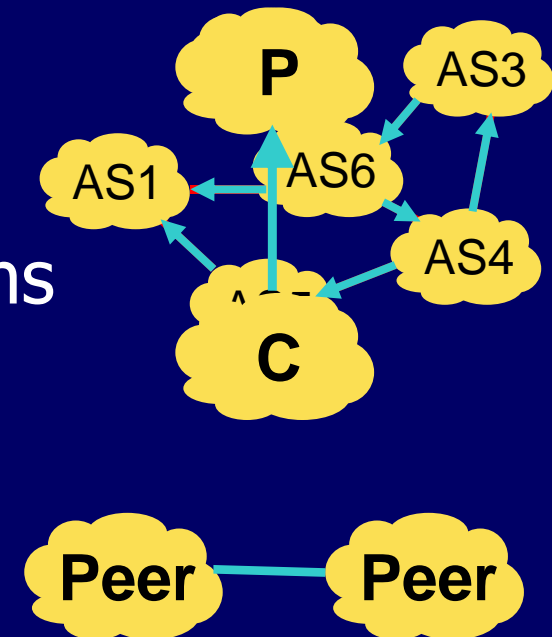
- vertices  $\Leftrightarrow$  ASes

- edges  $\Rightarrow$  BGP peering sessions

- ◆ Relationship assignment

↕

graph orientation



# Inference Algorithms

## ◆ State of the art

■ L. Gao. On Inferring Autonomous System Relationships in the Internet. *IEEE/ACM Transactions on Networking*, 9(6):733–745, Dec 2001.

degree-based

SARK

■ L. Subramanian, S. Agarwal, J. Rexford, and R.H. Katz. Characterizing the Internet Hierarchy from Multiple Vantage Points. In *Proc. IEEE INFOCOM 2002*.

ranking,  
multiple  
observation  
points

DPP

■ G. Di Battista, M. Patrignani, and M. Pizzonia. Computing the Types of the Relationships between Autonomous Systems. In *Proc. IEEE INFOCOM 2003*.

satisfiability of  
propositional  
formulae, no  
peerings



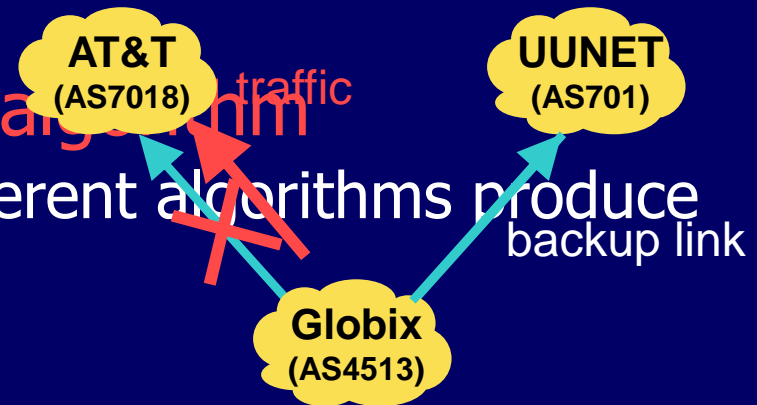
# Summary

- ♦ Introduction
  - ♦ Motivations
  - ♦ Methodology
  - ♦ Tools
  - ♦ Experimental Results
  - ♦ Conclusions

# Motivations

## ◆ Results Analysis

- do inference algorithms produce realistic results?
- **stability analysis**
  - evaluates the impact of routing oscillations on relationship assignments
- **independence from the algorithm**
  - investigates whether different algorithms produce similar results



## ◆ Model Validation

- good results  $\Rightarrow$  sound models

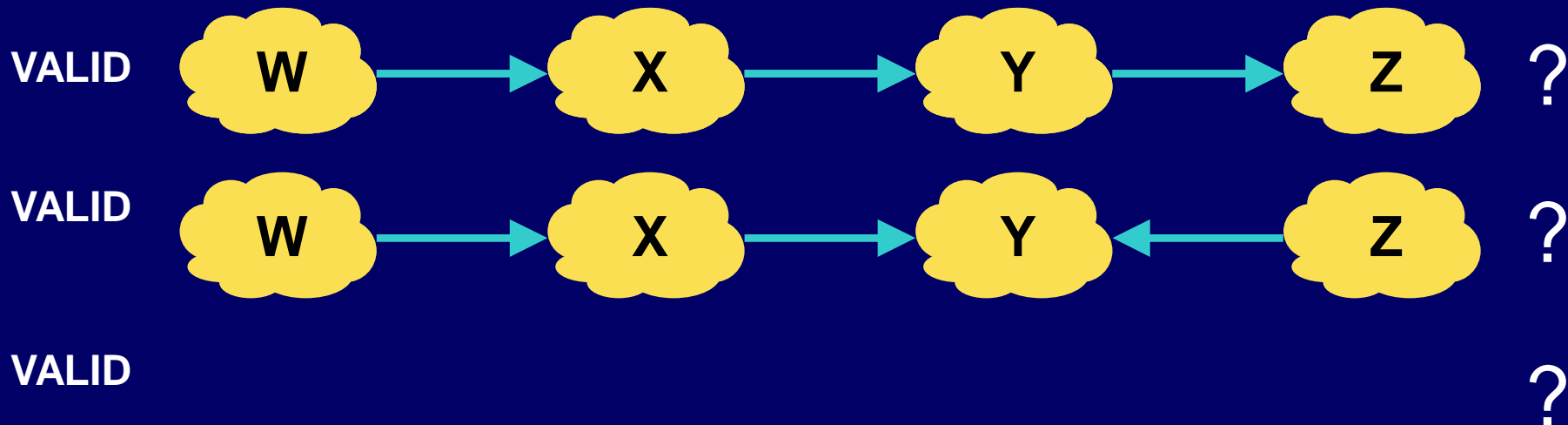
## ◆ Towards a unified methodology

# Methodology

## ✦ Possible approach:

- considering assignments as being realistic depending on the ability to enforce the valley-free property

## ✦ Drawback:



# Methodology

## ◆ Another possibility:

- validating assignments against real world data [1]

## ◆ Drawback:

- retrieving real world information is not easy
- not scalable

[1] Lixin Gao. On Inferring Autonomous System Relationships in the Internet. *IEEE/ACM Transactions on Networking*, 9(6):733–745, Dec 2001.

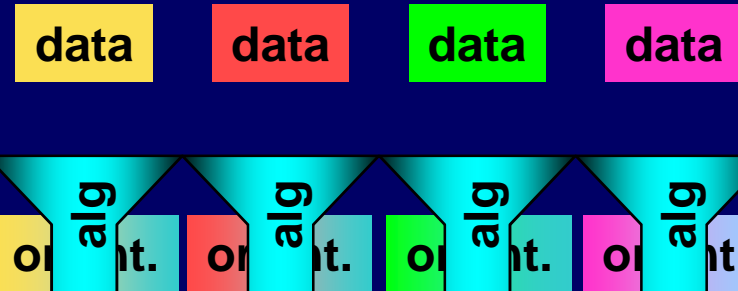
# Methodology

- ◆ Our approach:
  1. identify (other) qualities of a reasonably good inference
  2. define **measures** which evaluate such qualities
  3. run the inference algorithms extensively on several input data sets
  4. compute the measures on the relationship assignments that have been produced
  5. draw conclusions

# Methodology: Qualities

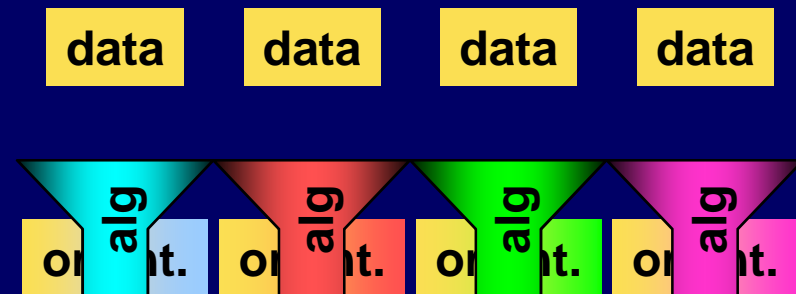
## ◆ Stability

- several time consecutive snapshots
- single algorithm



## ◆ Independence from the algorithm

- single snapshot
- different algorithms



# Methodology: Measures

- ◆ Undirected AS graph:  $G(V, E)$
- ◆ Relationship assignment on  $G$ :

$$R : E \rightarrow V \cup \{peering, unknown\}$$
$$R(e) = \begin{cases} AS_2 & \text{if } AS_2 \text{ is a provider of } AS_1 \\ AS_1 & \text{if } AS_1 \text{ is a provider of } AS_2 \\ peering & \text{if } AS_1 \text{ and } AS_2 \text{ are peers} \\ unknown & \text{if no relationship is known} \end{cases}$$

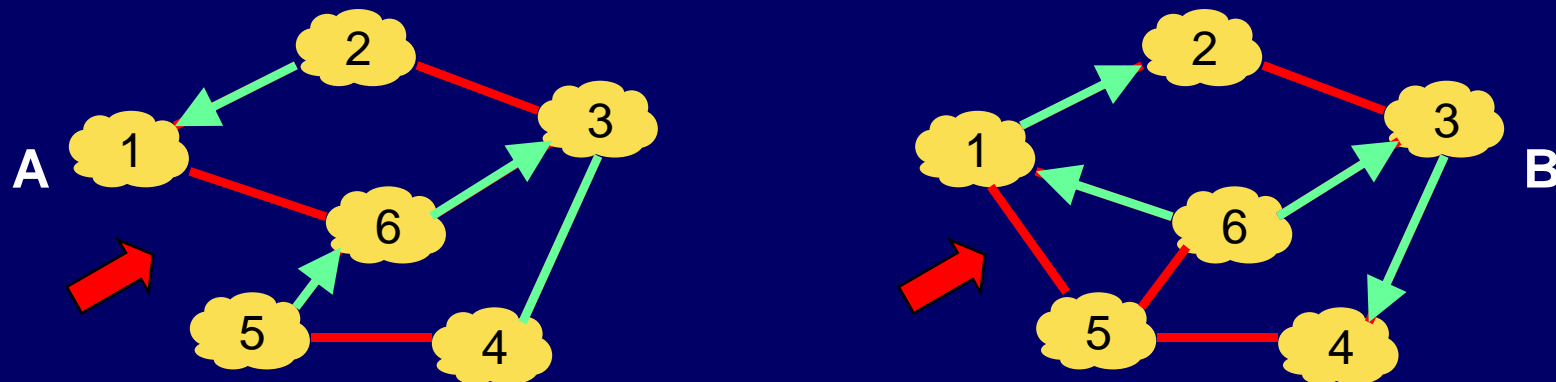
# Methodology: Measures

- Two relationship assignments,  $R_A(\cdot)$  and  $R_B(\cdot)$ , defined on the same graph

$$\text{Both} = \{e \in E \mid R_A(e) \neq \text{unknown} \wedge R_B(e) \neq \text{unknown}\}$$

$$\text{OnlyInA} = \{e \in E \mid R_A(e) \neq \text{unknown} \wedge R_B(e) = \text{unknown}\}$$

$$\text{OnlyInB} = \{e \in E \mid R_A(e) = \text{unknown} \wedge R_B(e) \neq \text{unknown}\}$$





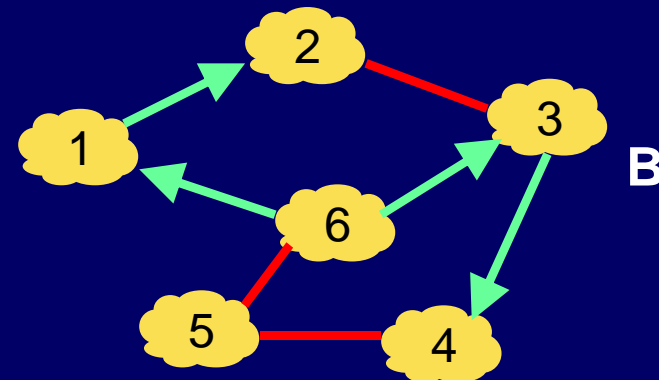
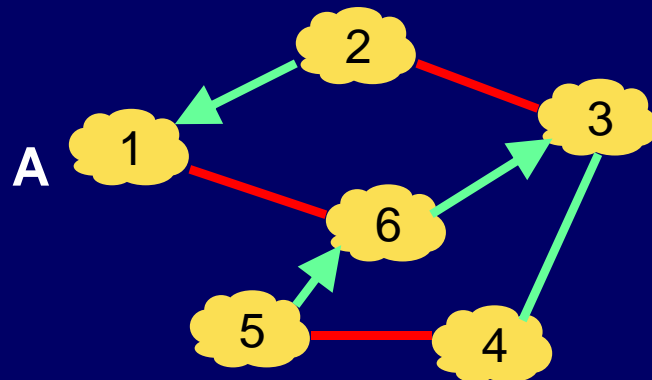
# Methodology: Measures

- Two relationship assignments,  $R_A(\cdot)$  and  $R_B(\cdot)$ , defined on the same graph

$$\text{Both} = \{e \in E \mid R_A(e) \neq \text{unknown} \wedge R_B(e) \neq \text{unknown}\}$$

$$\text{OnlyInA} = \{e \in E \mid R_A(e) \neq \text{unknown} \wedge R_B(e) = \text{unknown}\}$$

$$\text{OnlyInB} = \{e \in E \mid R_A(e) = \text{unknown} \wedge R_B(e) \neq \text{unknown}\}$$

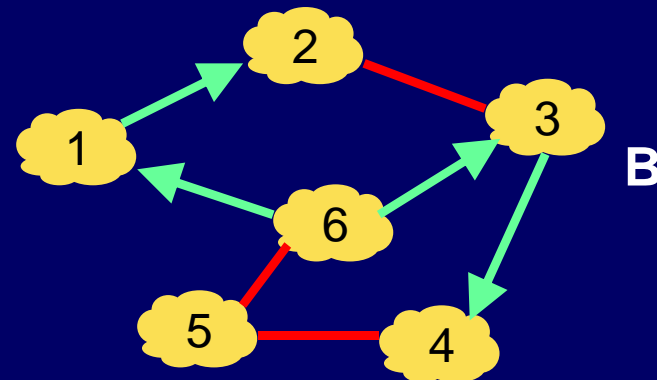
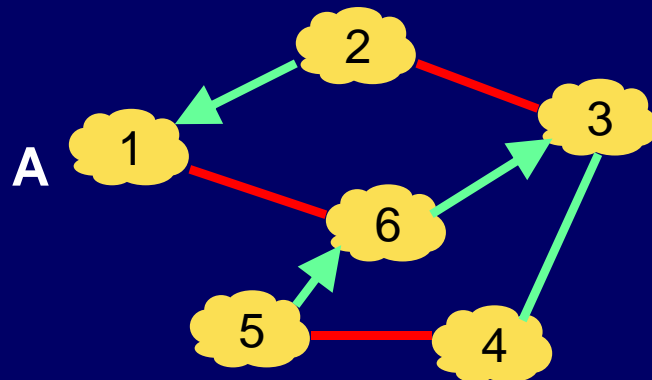


# Methodology: Measures

$Both = \{e \in E \mid R_A(e) \neq unknown \wedge R_B(e) \neq unknown\}$

$Consistent = \{e \in Both \mid R_A(e) = R_B(e)\}$

$Inconsistent = \{e \in Both \mid R_A(e) \neq R_B(e)\}$

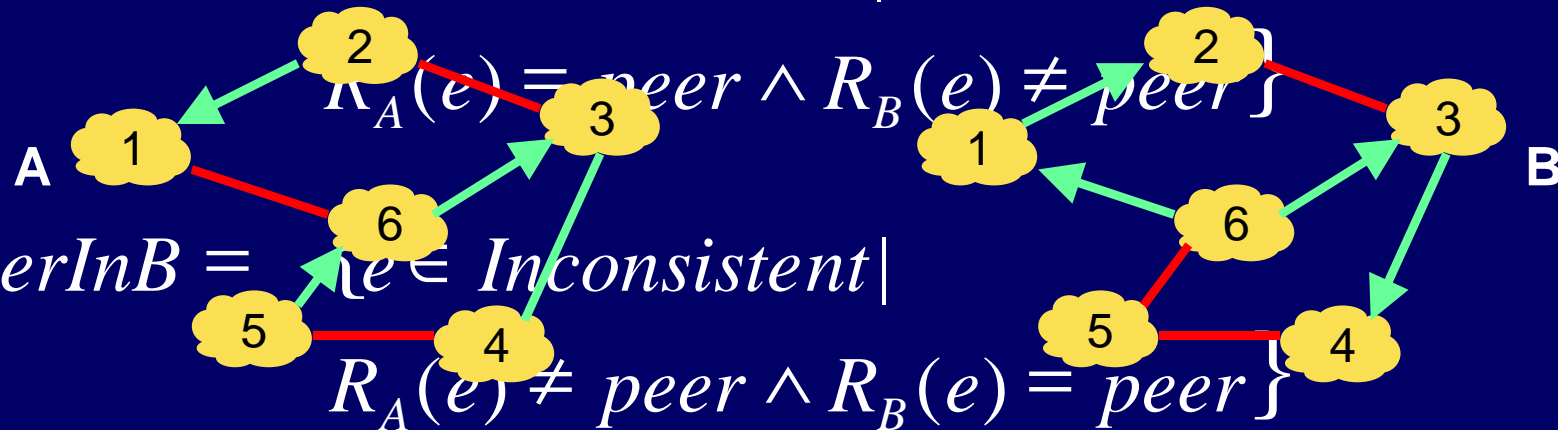


# Methodology: Measures

$$\text{Inconsistent} = \{e \in \text{Both} \mid R_A(e) \neq R_B(e)\}$$

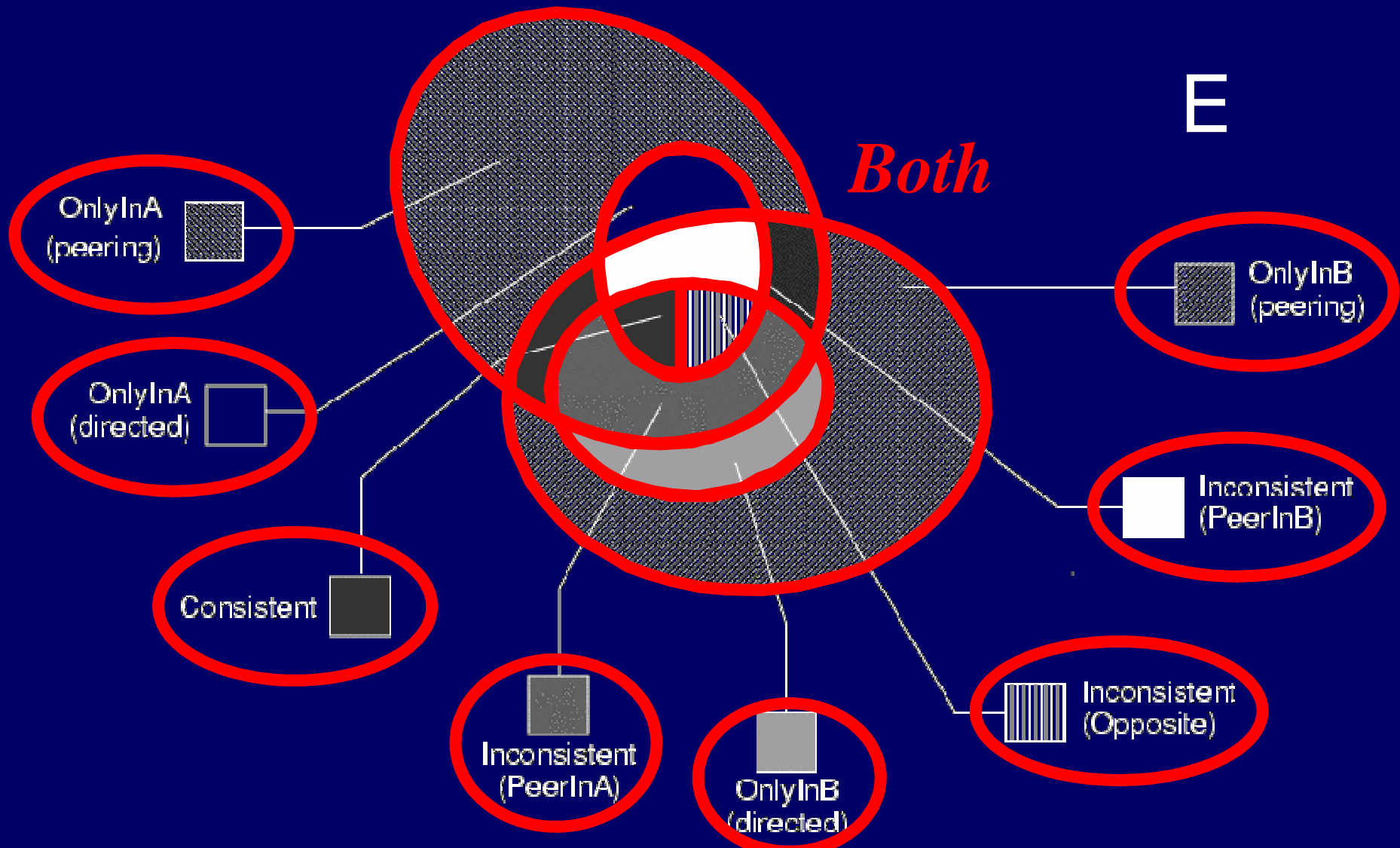
$$\text{Opposite} = \{e \in \text{Inconsistent} \mid R_A(e) \neq \text{peer} \wedge R_B(e) \neq \text{peer}\}$$

$$\text{PeerInA} = \{e \in \text{Inconsistent} \mid R_A(e) = \text{peer} \wedge R_B(e) \neq \text{peer}\}$$



$$\text{PeerInB} = \{e \in \text{Inconsistent} \mid R_A(e) \neq \text{peer} \wedge R_B(e) = \text{peer}\}$$

# Methodology: Measures



# Methodology: “Historical” Measures

✦ Sequence of AS graphs  $G_1(V_1, E_1), \dots, G_n(V_n, E_n)$

✦  $\tilde{G} = (\tilde{V}, \tilde{E})$

■  $\tilde{E} = \bigcup_{i=1}^n E_i$

■  $\tilde{V}$  is naturally induced by  $\tilde{E}$

✦ Sequence of relationship assignments

$R_1(\cdot), \dots, R_n(\cdot)$ , defined on  $\tilde{E}$

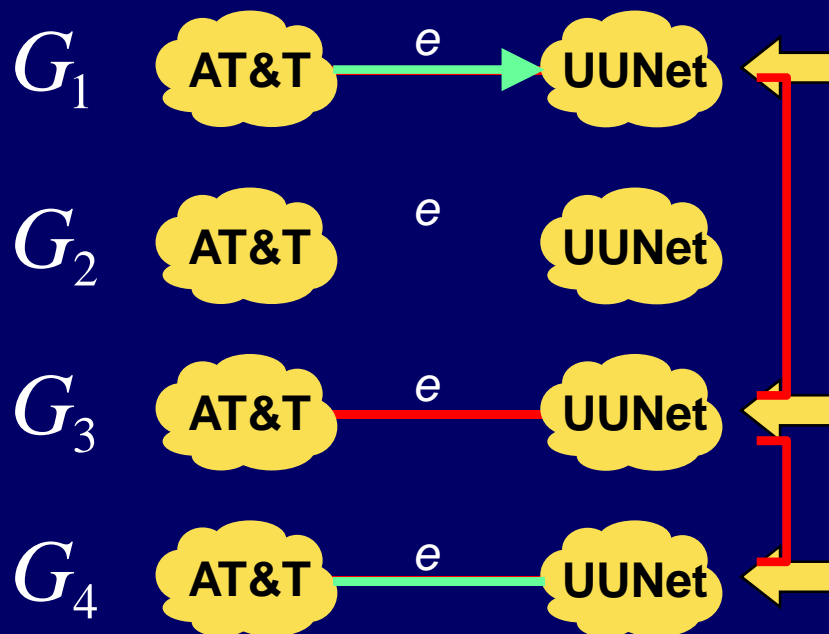
■ assumption:

$$\forall e \in \tilde{E} \setminus E_i : R_i(e) = \text{unknown}$$

# Methodology: "Historical" Measures

$$J(e) = \left\{ (j, k) \mid j, k \in \{1, \dots, n\} \wedge j < k \wedge \begin{array}{l} \text{Assignments}(e) = \{j, k\} \\ e \in E_j \cap E_k \wedge \forall h \in \{j+1, \dots, k-1\}: e \notin E_h \end{array} \right\}$$

$$\text{Changes}(e) = \left| \left\{ (i, j) \mid (i, j) \in J(e) \wedge R_i(e) \neq R_j(e) \right\} \right|$$



$$\text{Occurrences}(e) = 3$$

$$\text{Assignments}(e) = 2$$

$$\text{Changes}(e) = 2$$

# Summary

- ◆ Introduction
- ➔ ◆ Motivations
- ➔ ◆ Methodology
- ◆ Tools
- ◆ Experimental Results
- ◆ Conclusions

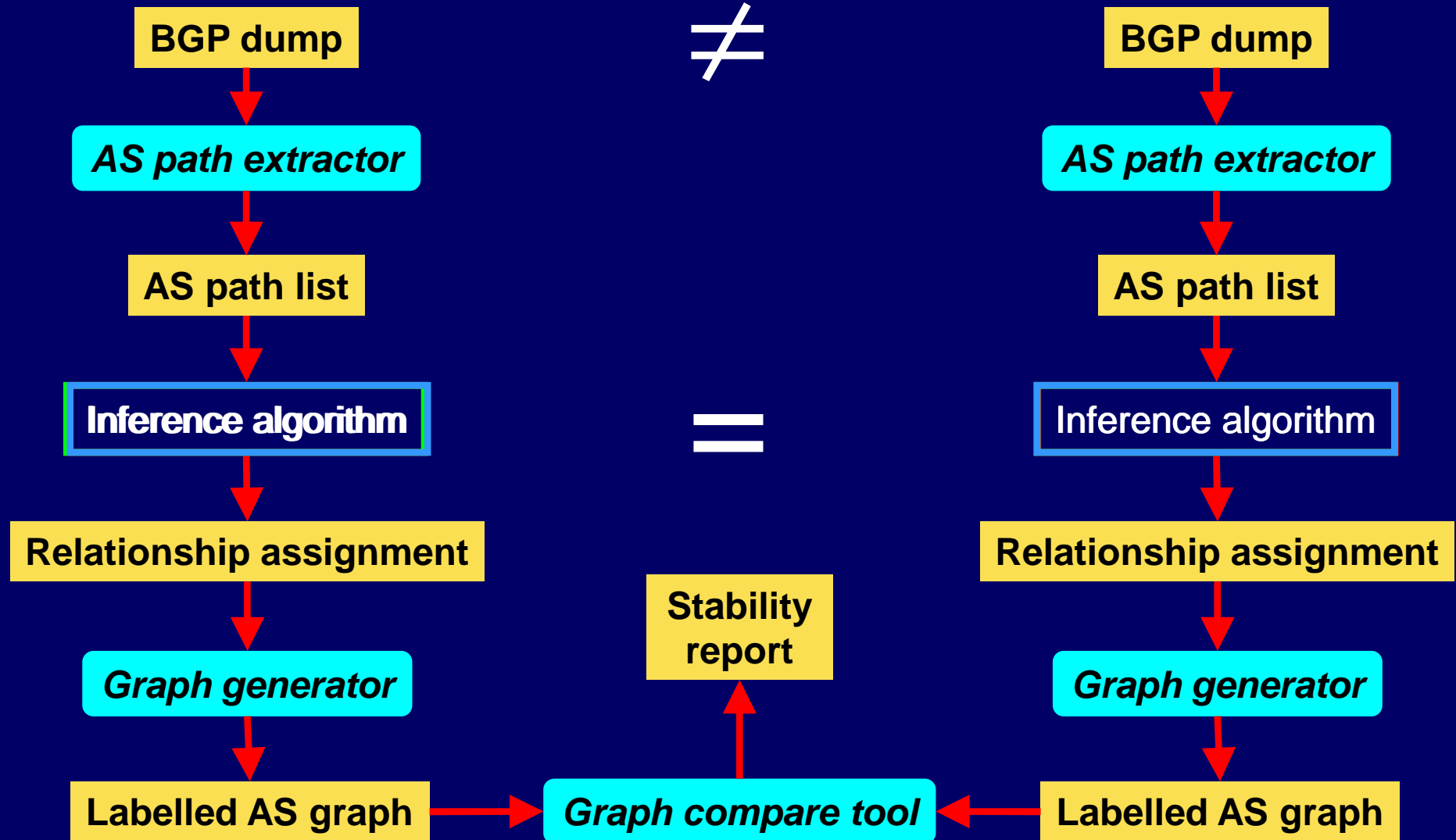
# Software Tools

- ✦ TORQUE (Type Of Relationship QUality Evaluation): four tools supporting the methodology [4]
  - **AS path extractor**: processes the data sets ('show ip bgp' dumps) to extract a list of AS paths from them (typical input of the inference algorithms)
  - **graph generator**: creates a labelled graph; each edge is associated with the value of  $R(\cdot)$
  - **graph compare tool**: computes the measures we have just defined
  - **graph view tool**: produces reports

[4] available for download at <http://www.dia.uniroma3.it/~compunet/torque>



# Software Tools: Usage



# Software Tools: Usage

BGP dump

*AS path extractor*

AS path list

Inference algorithm

Relationship assignment

*Graph generator*

Labelled AS graph



BGP dump

*AS path extractor*

AS path list

Inference algorithm

Relationship assignment

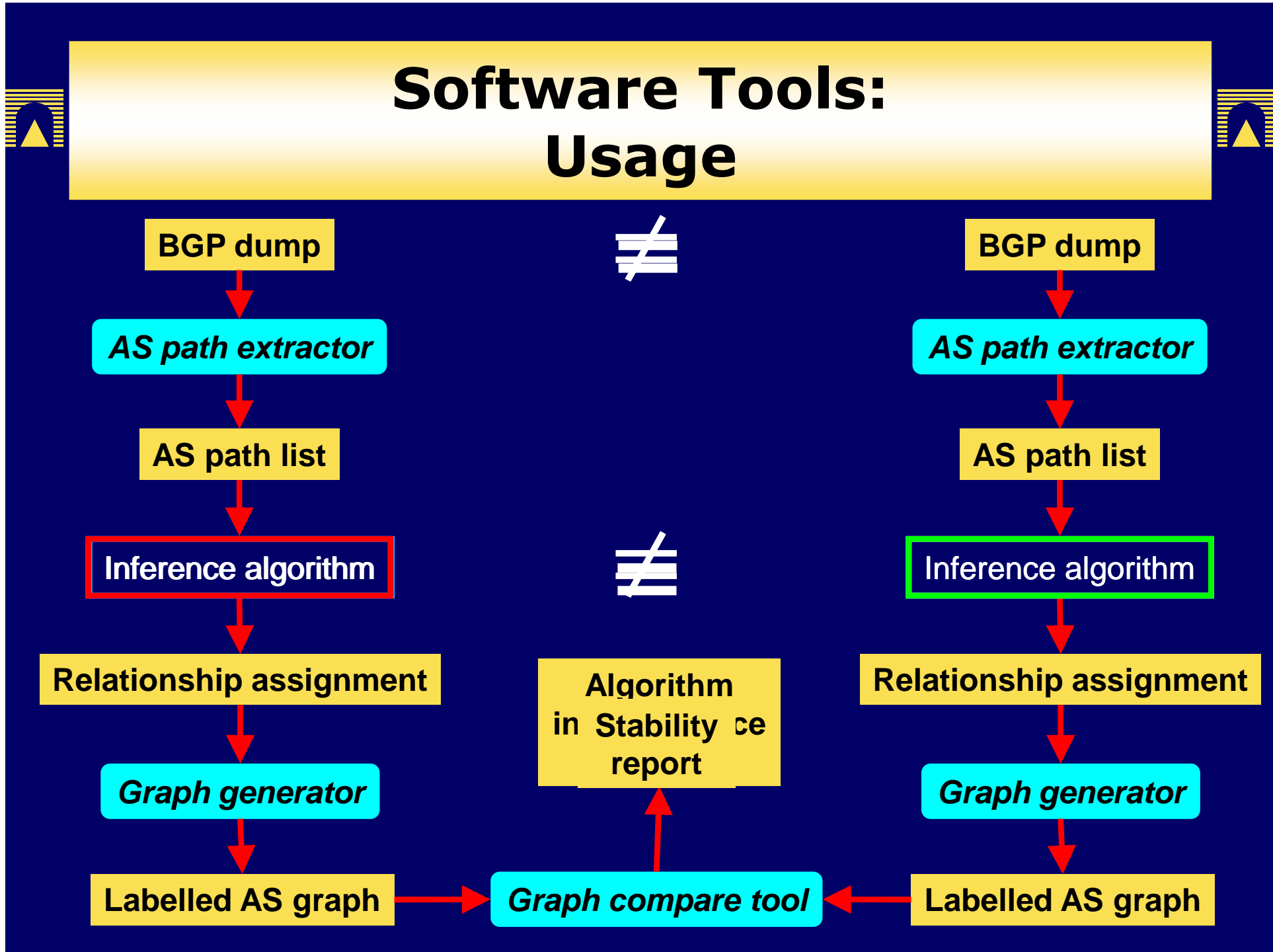
*Graph generator*

Labelled AS graph

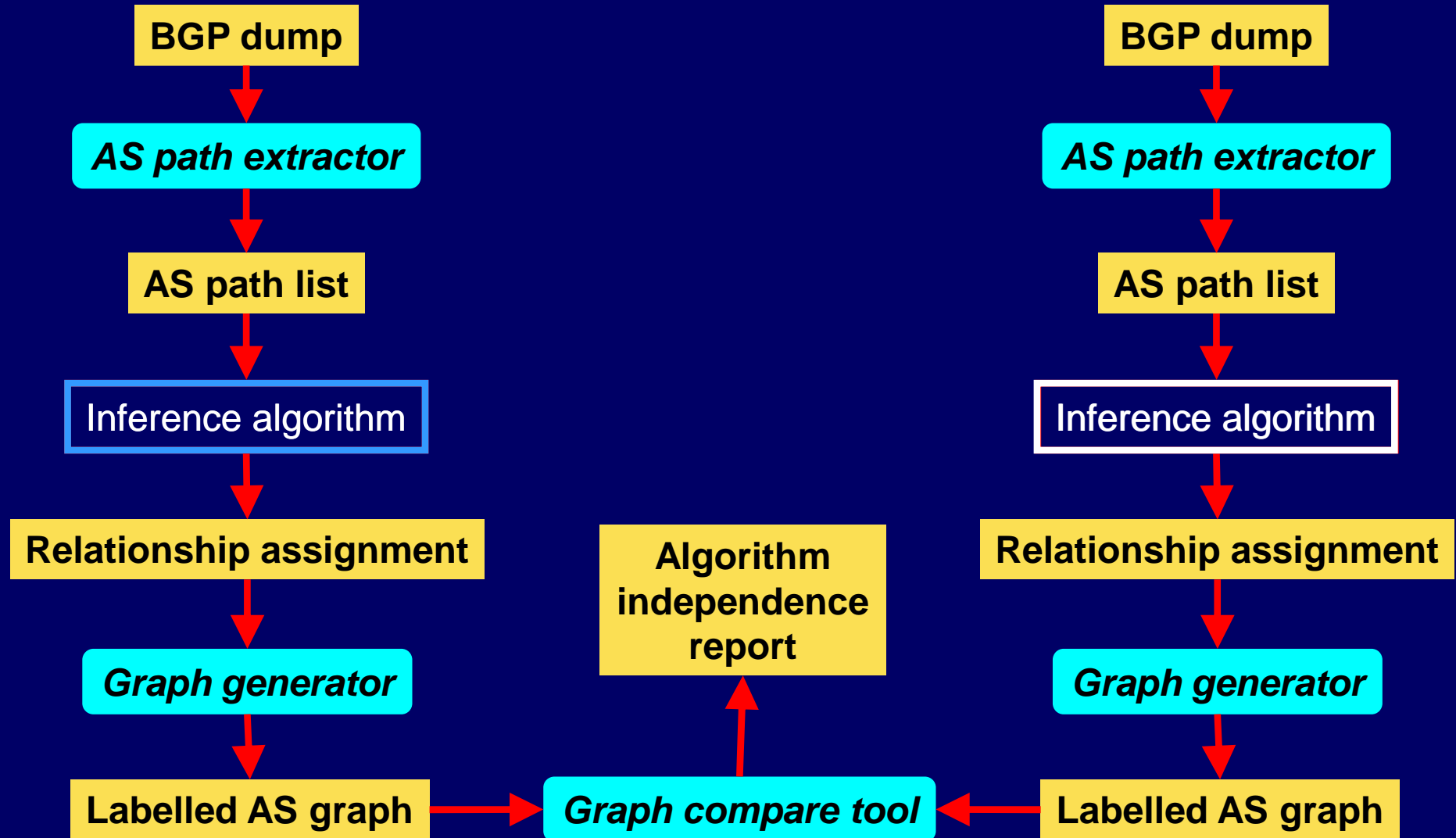


Algorithm  
in Stability ce  
report

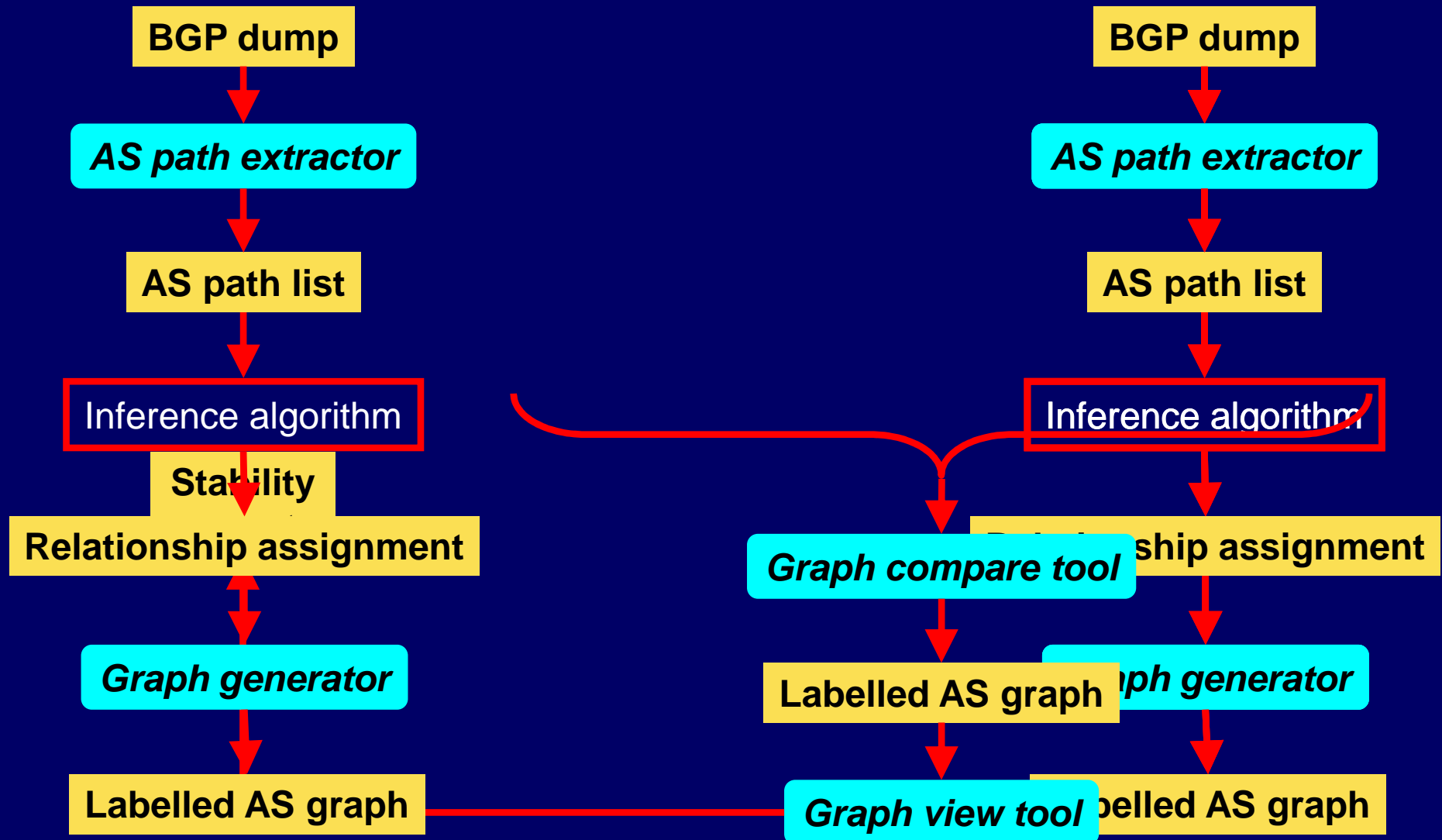
*Graph compare tool*



# Software Tools: Usage



# Software Tools: Usage



# Summary

- ◆ Introduction
- ◆ Motivations
- ◆ Methodology
- ➔ ◆ Tools
- ◆ Experimental Results
- ◆ Conclusions

# Experimental Results: Data sets

- ◆ <http://www.cs.berkeley.edu/>
  - provides snapshots collecting simultaneous BGP tables from various telnet looking glasses

MVP

Date	Used looking glasses	AS graph		Unique
		Vertices	Edges	AS paths
18 Apr 2001	1, 1740, 3549, 3582, 3967, 4197, 7018, 8220, 8709	10909	23817	511200
29 Jan, 04 Feb 2002	1, 3549, 3582, 3967, 4197, 7018, 8220, 8709	12708	27555	722481
06 Apr 2002	1, 1838, 3549, 3582, 3967, 4197, 5511, 7018, 8220, 8709, 15290	13079	28309	942382
29 Jul 2002	1, 1838, 3257, 3549, 3582, 3967, 4197, 5511, 7018, 8220, 8709, 15290	13705	29073	948720
09 Aug 2002	1, 1838, 3257, 3549, 3582, 4197, 5511, 7018, 8220, 15290	13754	29009	894396
19 Oct 2002	1, 1838, 3582, 3967, 5511, 7018, 8220, 15290	14113	29422	881836
29 Oct 2003	1, 50, 210, 553, 852, 1838, 3257, 3549, 3582, 3741, 3967, 4197, 5388, 5511, 6395, 6539, 6893, 7018, 8220, 8709, 8843, 9328, 15290	16420	37470	1143373
13 Nov 2003	1, 50, 210, 553, 852, 1838, 3257, 3549, 3582, 3741, 3967, 4197, 5388, 5511, 6395, 6539, 6893, 7018, 8220, 8709, 8843, 9328, 15290	16461	37406	1157802
28 Nov 2003	1, 50, 210, 553, 852, 1838, 3257, 3549, 3582, 3741, 3967, 4197, 5388, 5511, 6395, 6539, 6893, 7018, 8220, 8709, 8843, 9328, 15290	16316	31419	247691
12 Dec 2003	1, 50, 210, 553, 852, 1838, 3257, 3549, 3582, 3741, 3967, 4197, 5388, 5511, 6395, 6539, 6893, 7018, 8220, 8709, 8843, 9328, 15290	16585	37790	1216534
29 Dec 2003	1, 50, 210, 553, 852, 1838, 3257, 3549, 3582, 3741, 3967, 4197, 5388, 5511, 6395, 6539, 6893, 7018, 8220, 8709, 8843, 9328, 15290	16728	38162	1164370
13 Jan 2004	1, 50, 210, 553, 852, 1838, 3257, 3549, 3582, 3741, 3967, 4197, 5388, 5511, 6395, 6539, 6893, 7018, 8220, 8709, 8843, 9328, 15290	16762	38205	1264677



# Experimental Results: Data sets

- ◆ University of Oregon RouteViews project.  
<http://www.routeviews.org>.
  - provides dumps of the RIB of a router having about 50 active peering sessions at the time of the experiments

	Start	End	# of snapshots
<b>RV1</b>	25 Mar 2003 00:00	31 Mar 2003 22:00	84
<b>RV2</b>	25 Sep 2001 00:00	08 Oct 2001 22:00	168

- RV1: few commercial changes
  - RV2: many commercial changes
  - Snapshots collected every 2 hours
- } sources: [5, 6]

[5] xSP Archives. <http://www.internetnews.com>

[6] ISP Business: Archives. <http://isp-planet.com/>

# Experimental Results: Stability Analysis

- ✦ (A),(B): pair of consecutive snapshots
- ✦  $R(\cdot)$  is defined on the intersection of  $G_A$  and  $G_B$
- ✦ Data set: MVP
- ✦ Algorithm: DPP
- ✦ PeerInA, PeerInB are omitted

	18 Apr 2001 (A)	29 Jul 2002 (A)	09 Aug 2002 (A)
	29 Jan, 04 Feb 2002 (B)	09 Aug 2002 (B)	19 Oct 2002 (B)
OnlyInA	7	5	3
OnlyInB	18	1	2
Both	15919	28039	25458
Consistent	15118 (95%)	27719 (99%)	24916 (98%)
Inconsistent	801 (5%)	320 (1%)	542 (2%)

- ✦ Very good stability (>95%)

	13 Nov 2003 (A)	28 Nov 2003 (A)	12 Dec 2003 (A)
	28 Nov 2003 (B)	12 Dec 2003 (B)	29 Dec 2003 (B)
OnlyInA	4	4	7
OnlyInB	2	2	2
Both	30654	31034	37038
Consistent	30120 (98%)	30509 (98%)	36653 (99%)
Inconsistent	534 (2%)	525 (2%)	385 (1%)



# Experimental Results: Stability Analysis

- ✦ Data set: MVP
- ✦ Algorithm: SARK

✦ Very good stability (>96%)

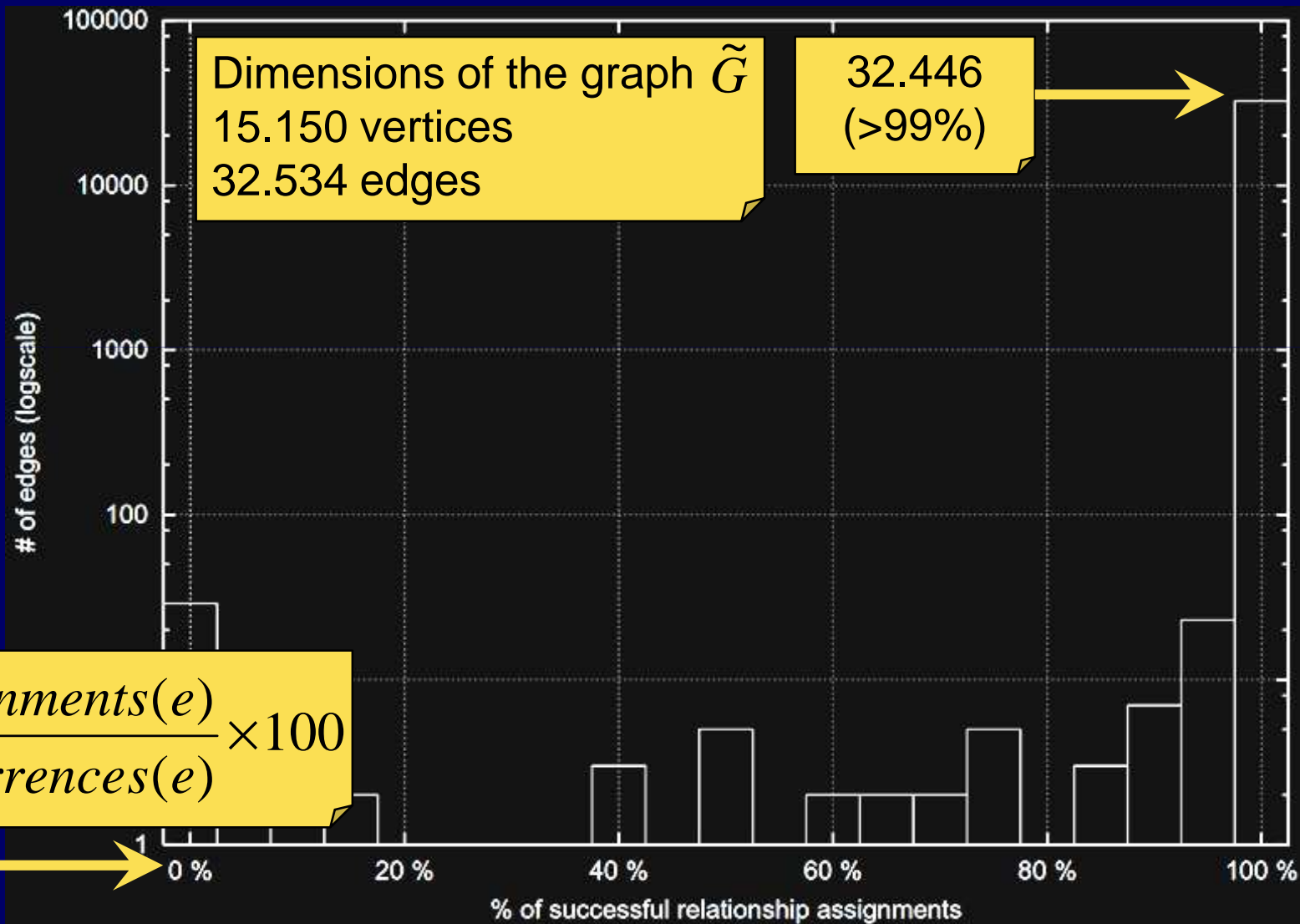
✦ Most changes are due to the appearance or disappearance of peerings

	18 Apr 2001 (A)	29 Jul 2002 (A)	09 Aug 2002 (A)
	29 Jan, 04 Feb 2002 (B)	09 Aug 2002 (B)	19 Oct 2002 (B)
OnlyInA	86	80	111
OnlyInB	77	94	89
Both	15749	27789	25224
Consistent	15056 (96%)	27343 (98%)	24425 (97%)
Inconsistent	693 (5%)	446 (2%)	799 (3%)
Opposite	55 (8%)	14 (3%)	44 (6%)
PeerInA	350 (51%)	257 (57%)	367 (46%)
PeerInB	288 (41%)	175 (40%)	388 (48%)

	13 Nov 2003 (A)	28 Nov 2003 (A)	12 Dec 2003 (A)
	28 Nov 2003 (B)	12 Dec 2003 (B)	29 Dec 2003 (B)
OnlyInA	613	64	157
OnlyInB	58	599	168
Both	29099	29482	35739
Consistent	28743 (99%)	29146 (99%)	35100 (98%)
Inconsistent	351 (1%)	336 (1%)	639 (2%)
Opposite	8 (2%)	2 (1%)	10 (2%)
PeerInA	237 (68%)	103 (31%)	346 (54%)
PeerInB	106 (30%)	231 (68%)	283 (44%)

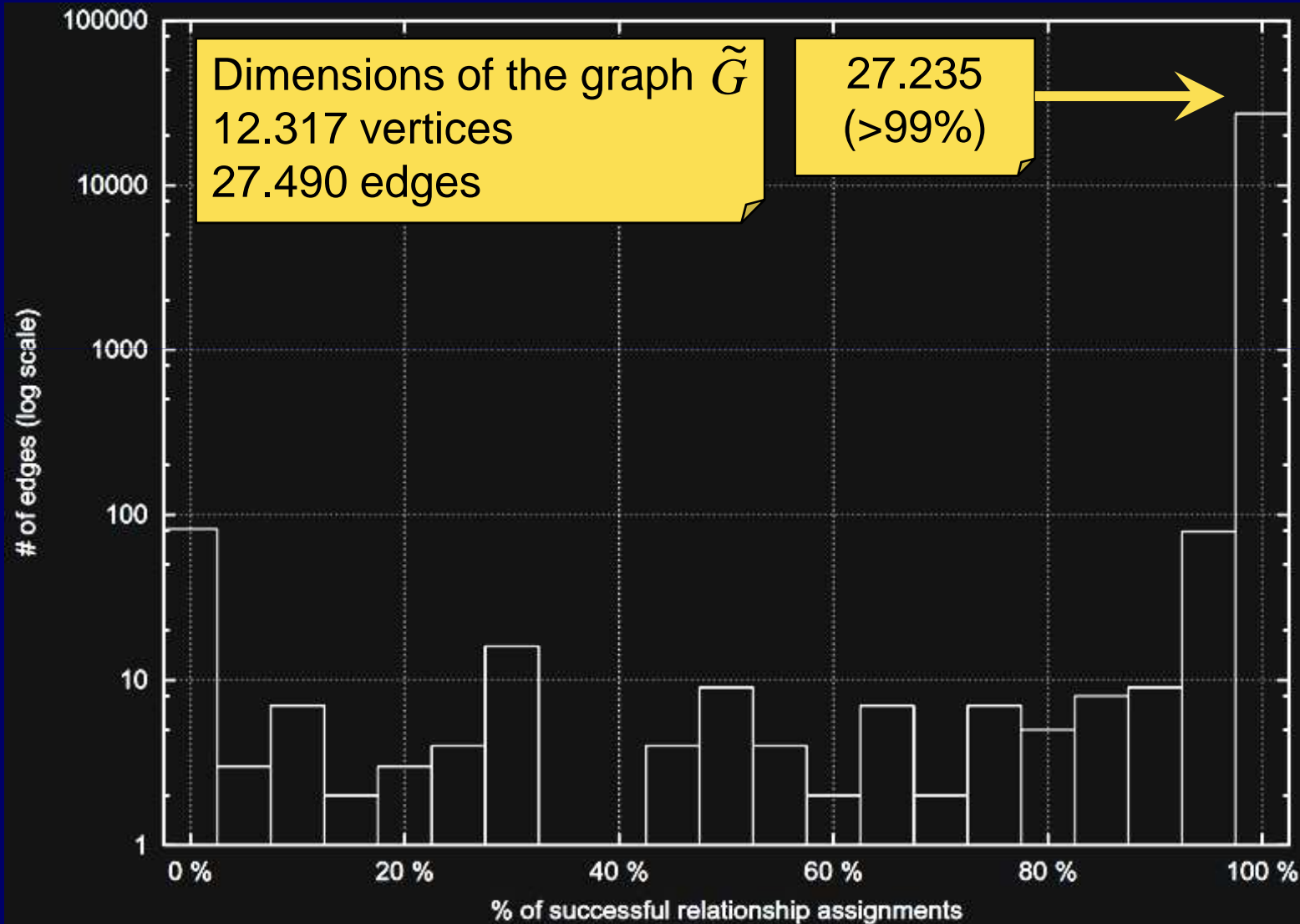
# Experimental Results: Stability Analysis

RV1  
DPP



# Experimental Results: Stability Analysis

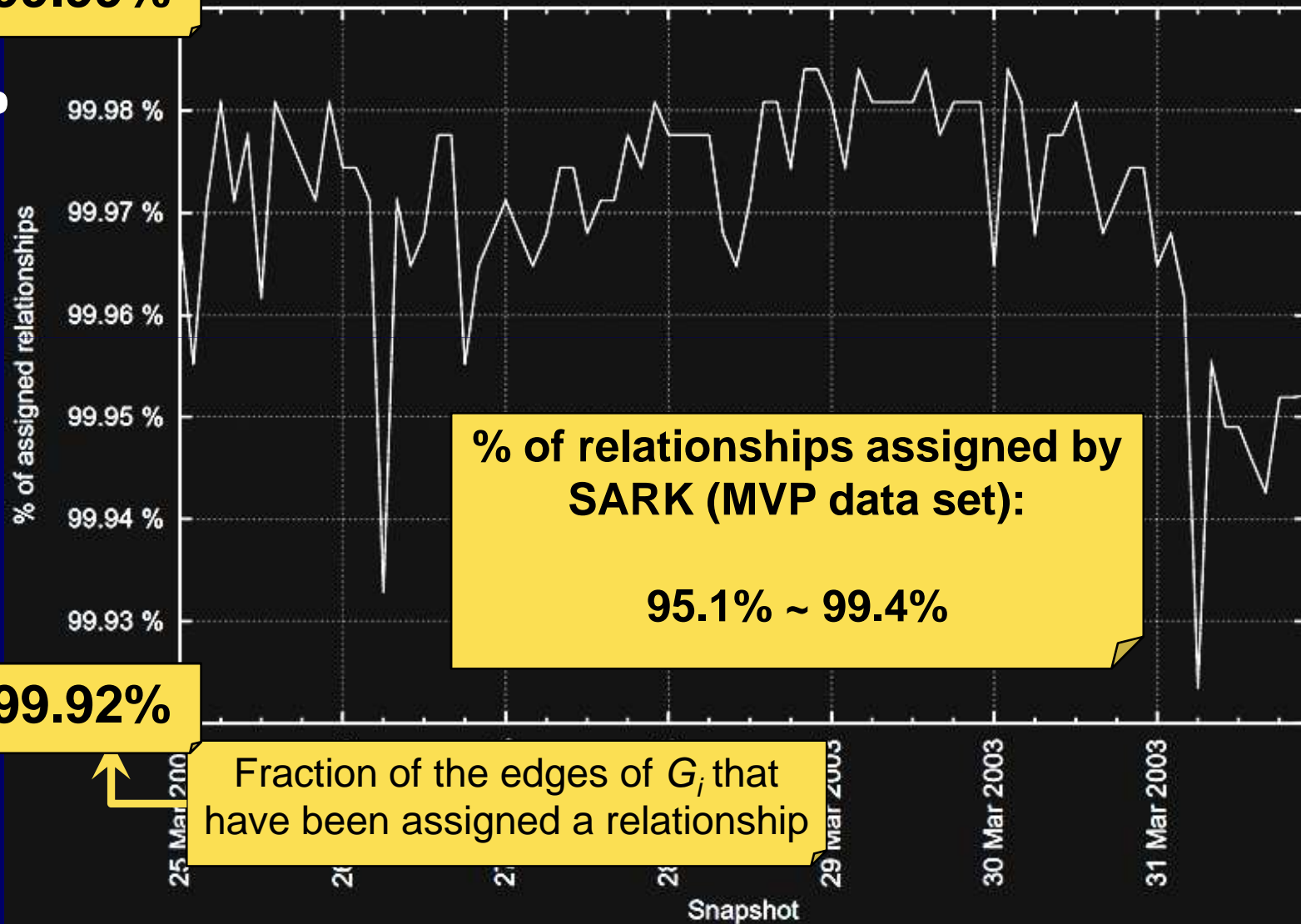
RV2  
DPP



# Experimental Results: Stability Analysis

99.99%

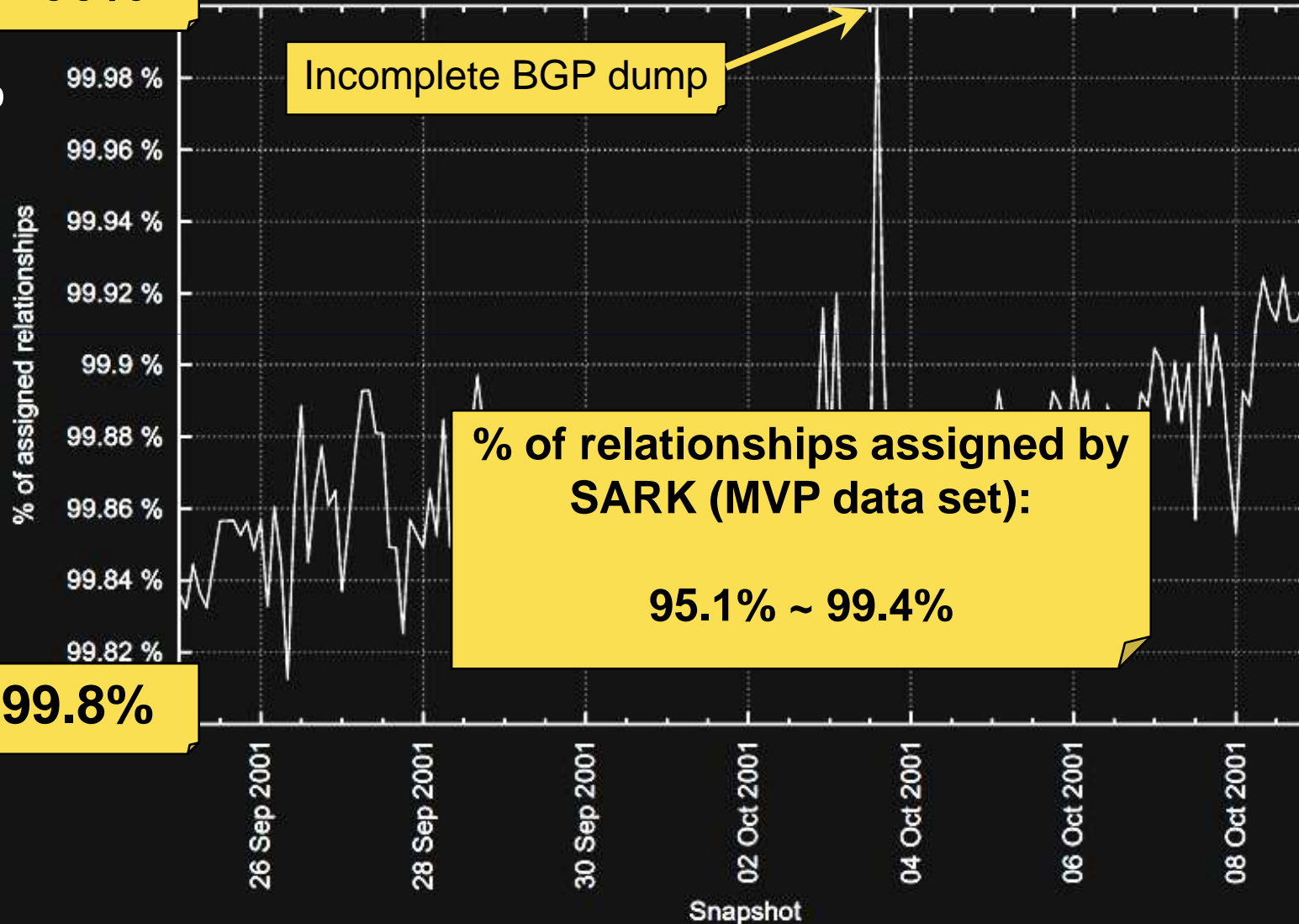
RV1  
DPP



# Experimental Results: Stability Analysis

100%

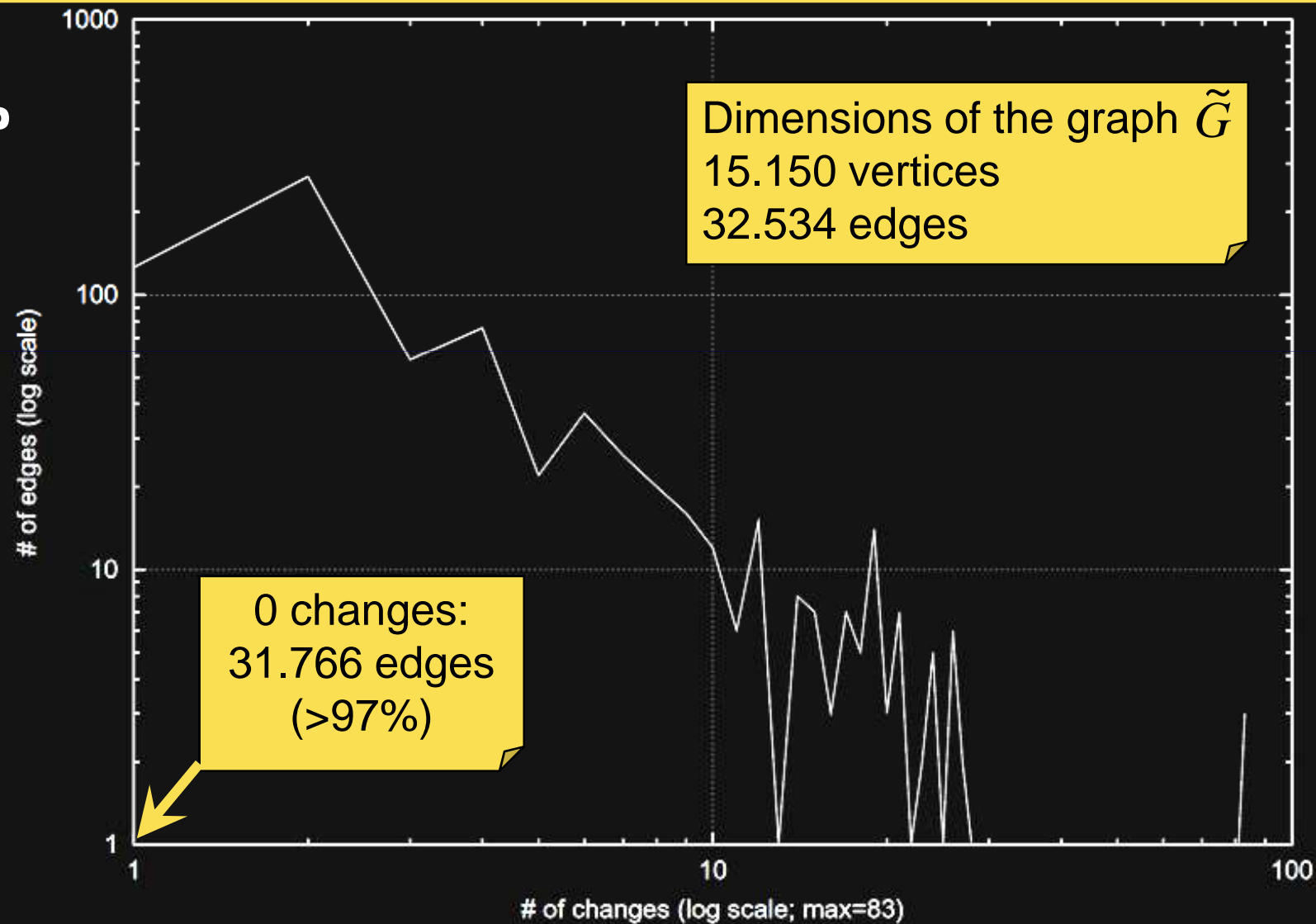
RV2  
DPP



99.8%

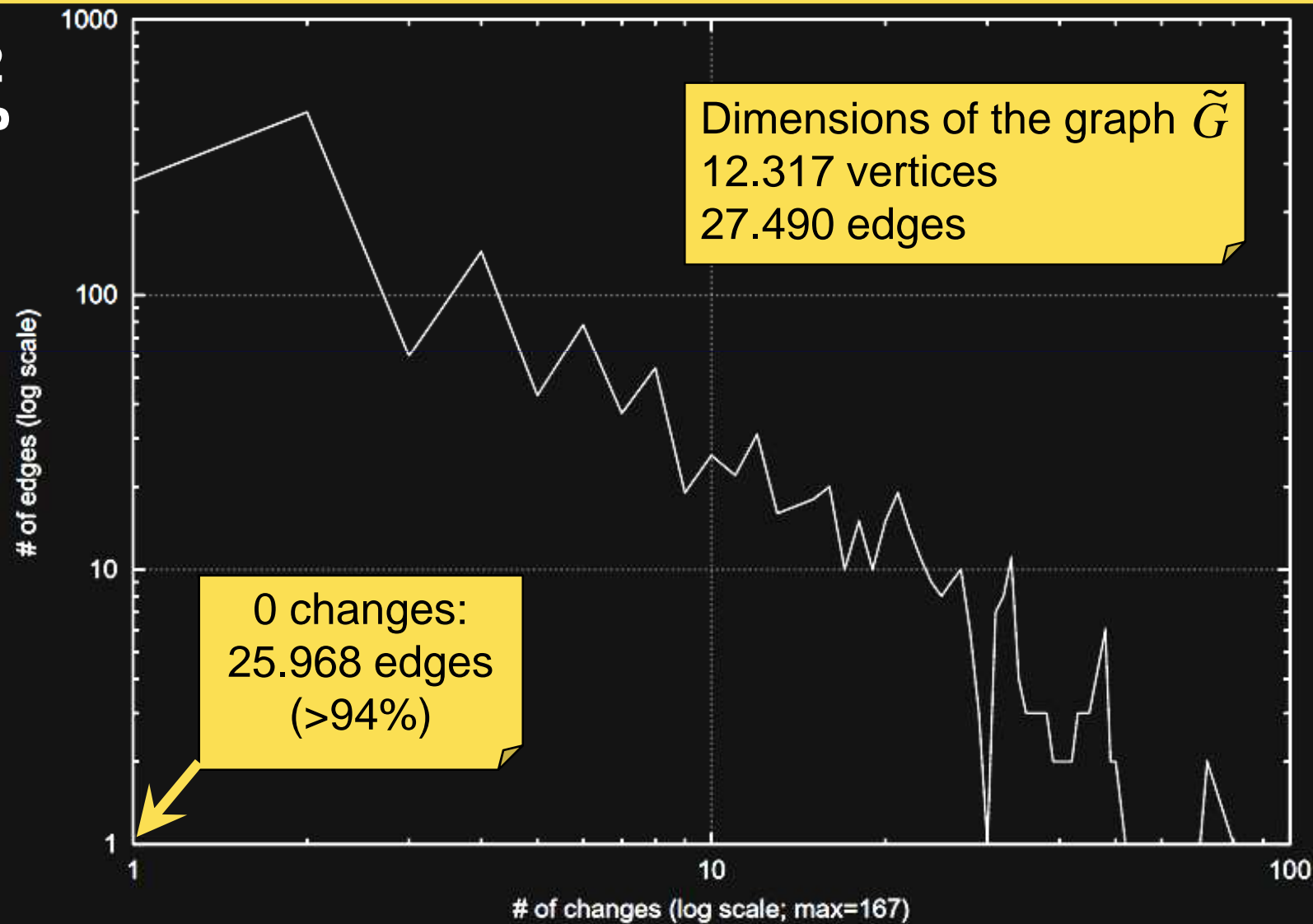
# Experimental Results: Stability Analysis

RV1  
DPP



# Experimental Results: Stability Analysis

RV2  
DPP



# Experimental Results: Independence from the Algorithm

- ✦ (A): DPP algorithm
- ✦ (B): SARK algorithm
- ✦ Data set: MVP
- ✦  $R(\cdot)$  is defined on the intersection of  $G_A$  and  $G_B$
- ✦ PeerInA is omitted
- ✦ Fair independence (>90%)
- ✦ Differences are equally shared between c-p and p-p

	18 Apr 2001	29 Jan, 04 Feb 2002	29 Jul 2002	19 Oct 2002
OnlyInA	192	213	200	196
OnlyInB	39	21	6	14
Both	23584	27317	28866	29212
Consistent	21487 (91%)	24997 (91%)	26267 (91%)	26659 (91%)
Inconsistent	2097 (9%)	2320 (9%)	2605 (9%)	2553 (9%)
Opposite	993 (47%)	1047 (45%)	1176 (45%)	1247 (49%)
PeerInB	1104 (53%)	1279 (55%)	1429 (55%)	1306 (51%)

	29 Oct 2003	13 Nov 2003	28 Nov 2003	12 Dec 2003
OnlyInA	1205	1173	1548	1367
OnlyInB	28	25	5	12
Both	36235	36208	29866	36409
Consistent	32683 (90%)	32657 (90%)	28332 (95%)	32754 (90%)
Inconsistent	3552 (10%)	3551 (10%)	1534 (5%)	3655 (10%)
Opposite	1689 (48%)	1738 (49%)	829 (54%)	1783 (49%)
PeerInB	1863 (52%)	1819 (51%)	705 (46%)	1872 (51%)



# Summary

- ◆ Introduction
- ◆ Motivations
- ◆ Methodology
- ◆ Tools
- ➔ ◆ Experimental Results
- ◆ Conclusions

# Conclusions

- ✦ Analysis of (the results of) state-of-the-art algorithms for the inference of commercial relationships between Autonomous Systems
  - stability analysis
  - independence from the algorithm
- ✦ A new methodology
  - a set of measures
  - a procedure (and software tools) to compute them
- ✦ Application of the methodology
  - stability analysis: DPP and SARK
  - independence from the algorithm: DPP against SARK
- ✦ Outcome of the analysis
  - very good stability (>94%)
  - fair independence from the algorithm (>90%)
- ✦ Based on this work, we think (these) inference algorithms are trustworthy

# Future Work

- ✦ Analyzing the results produced by the algorithm in [1]
- ✦ Degrees of freedom
- ✦ Game theory
- ✦ ...

[1] Lixin Gao. On Inferring Autonomous System Relationships in the Internet. *IEEE/ACM Transactions on Networking*, 9(6):733–745, Dec 2001.